

Test 1 - Model answer

TEST 1 (EEE 241)

1. $W_B = 10 \mu\text{m}$, $I_C = 0.5 \text{mA}$
E-B depletion capacitance, $C_{je} = 2 \text{pF}$

$$\tau_F = \frac{W_B^2}{2D_p}$$

Neglect C-B capacitance, C_{μ} .

Diffusion coefficient of minority carrier in B
of a pnp transistor is $D_p = 13 \text{cm}^2/\text{s}$

$$V_T = 26 \text{mV}$$

Find f_T ?

Solution

$$f_T = \frac{1}{2\pi} \frac{g_m}{C_{\pi} + C_{\mu}}$$

$$C_{\pi} = C_b + C_{je}$$

Base charging capacitance, $C_b = \tau_F g_m$

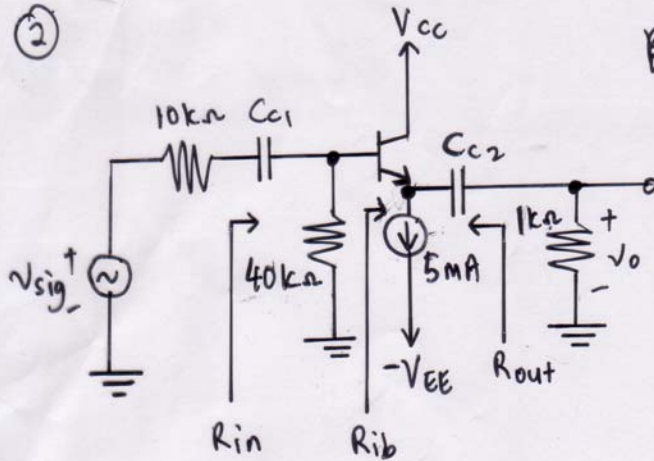
$$\tau_F = \frac{(10 \mu\text{m})^2}{2(13 \text{cm}^2/\text{s})} = \frac{(0.001 \text{cm})^2}{26 \text{cm}^2/\text{s}} = 38.4615 \text{ns} \quad (1)$$

$$g_m = \frac{I_C}{V_T} = \frac{0.5 \text{mA}}{26 \text{mV}} = 0.0192 \text{A/V} \quad (1)$$

$$\therefore C_b = 38.4615 \text{ns} \times 0.0192 \text{A/V} = 0.7385 \text{nF} \quad (1)$$

$$f_T = \frac{1}{2\pi} \frac{0.0192 \text{A/V}}{(0.7385 \text{nF} + 0.002 \text{nF})} = 4.1266 \text{MHz} \quad (2)$$

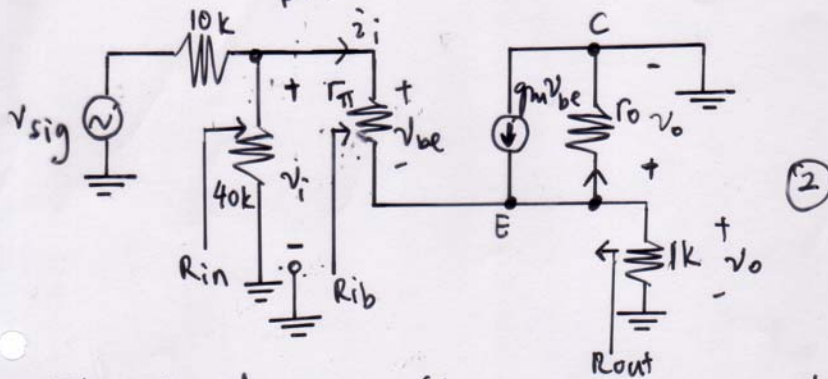
②



$\beta_F = \beta_0 = 100$
 $V_A = 100V$
 $V_T = 26mV$

$I_E = 5mA$

$I_C = \alpha I_E = \frac{\beta}{\beta+1} I_E = 4.9505 mA$ (2)



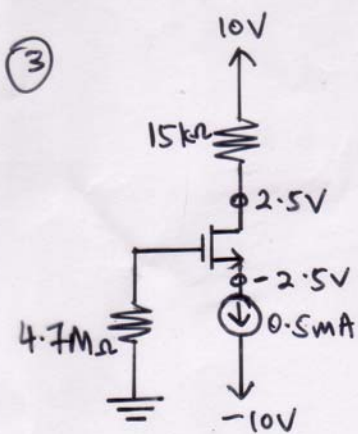
$R_{ib} = \frac{v_i}{i_i} = \frac{v_{be} + v_o}{i_i} = \frac{(v_{be} + v_o) r_{\pi}}{v_{be}} = r_{\pi} + \frac{v_o}{v_{be}} r_{\pi}$ (2)

KCL at node E, $g_m v_{be} + \frac{v_{be}}{r_{\pi}} = v_o \left(\frac{1}{r_o} + \frac{1}{1k} \right)$ (2)

$\therefore v_o = \frac{v_{be} \left(g_m + \frac{1}{r_{\pi}} \right)}{\frac{1}{r_o} + \frac{1}{1k}}$ (1) $g_m = \frac{I_C}{V_T} = \frac{4.9505mA}{26mV}$

$\therefore R_{ib} = r_{\pi} + \frac{\left(g_m + \frac{1}{r_{\pi}} \right) r_{\pi}}{\frac{1}{r_o} + \frac{1}{1k}} = 96.7615 k\Omega$ (2) # $\therefore g_m = 0.1904 A/V$

$R_{in} = 40k \parallel R_{ib} = 28.3008 k\Omega$ (2) # (1) $r_o = \frac{V_A}{I_C} = \frac{100V}{4.9505mA} = 20.2k\Omega$
 (1) $r_{\pi} = \beta_0 / g_m = 525.21 \Omega$



Given: $V_t = 1.5V$

$$I_D = 0.5mA$$

$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{ov})^2 (1 + \lambda V_{os}) \quad (1)$$

$$0.5m = \frac{1m}{2} (V_{ov})^2 (1 + \lambda V_{os})$$

$$\lambda = \frac{1}{75} \text{ since } V_A = 75V$$

$$V_{os} = V_D - V_S = 2.5 + 2.5 = 5V \quad (1)$$

$$\begin{aligned} \therefore V_{ov} &= \sqrt{\frac{0.5m \times 2}{1m \left[1 + \frac{1}{75}(5)\right]}} \\ &= \sqrt{\frac{1}{1.0667}} \\ &= \cancel{0.9375}^{0.9682} V \# \quad (1) \end{aligned}$$

$$V_{ov} = V_{GS} - V_t$$

$$V_{GS} = V_{ov} + V_t = \cancel{0.9375}^{0.9682} V + 1.5V = 2.4\cancel{275}^{682} V \#$$

$$V_{GS} = V_G - V_S$$

$$V_S = -2.5V \# \quad (1)$$

$$\therefore V_G = V_{GS} + V_S = \cancel{2.4275}^{2.4682} - 2.5 = -0.0\cancel{275}^{318} V \# \quad (2)$$

$$V_D = 2.5V \# \quad (1)$$

$$g_m = \mu_n C_{ox} \frac{W}{L} V_{ov} (1 + \lambda V_{os}) = 1m \left(\cancel{0.9375}^{0.9682}\right) \left(1 + \frac{5}{75}\right) = 1mS \# \quad (2)$$

$$r_o = \frac{1}{\lambda I_D} = \frac{75}{0.5m} = 150k\Omega \# \quad (1)$$